

3 flow  $\sim$   $\sim$

Amortized

$\sim$   $\sim$   $\sim$   $\sim$   $\sim$   $\sim$   $\sim$

$\sim$   $\sim$   $\sim$   $\sim$   $\sim$

Amortized time  $\frac{\text{time for w.c. series}}{\text{series length}}$

1.  $\sim$   $\sim$   $\sim$   $\sim$   $\sim$   $\sim$   $\sim$

2.  $\sim$   $\sim$   $\sim$   $\sim$   $\sim$   $\sim$   $\sim$

$\sim$   $\sim$   $\sim$   $\sim$   $\sim$

3.  $\sim$   $\sim$   $\sim$



$\sim$   $\sim$   $\sim$   $\sim$

increment:  ~~$\sim$~~

$i \leftarrow 1$

while ( $A[i] = 1$ )

$A[i] \leftarrow 0$

$i \leftarrow i + 1$

end while

$A[i] = 1$

Amortized =  $\frac{O(h)}{n} = O(1)$

$n + \frac{h}{2} + \frac{h}{4} + \dots + 2 + 1 \leq 2h$

$(1 - \frac{1}{2})(1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} \dots) = 1$

$1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} \dots = \frac{1}{1 - \frac{1}{2}} = 2$

$c_i \rightarrow c_i$   
 deposit withdrawal  
 deposit withdrawal

$$c_i^* = c_i + \text{deposit} - \text{withdrawal}$$

$$\sum_{i=1}^n c_i^* \geq \sum_{i=1}^n c_i$$

deposit withdrawal = 1 flow (deposit)

withdrawal = 0 or 1 flow (withdrawal)

increment ~~of~~ ~~the~~ flow

deposit of 1 or 0 flow

withdrawal of 1 or 0 flow

increment of deposit flow

1 or 0 flow

increment of deposit flow

$$\Phi(001010) = 2$$

deposit flow

$$\Phi(D_0) = 0$$

$$\Phi(D_n) \geq 0$$

$$\Phi(00000) = 0 = \Phi(D_0)$$

$\Phi(D_i)$  = number of deposit flows

$$c_i^* = c_i + \Phi(D_i) - \Phi(D_{i-1})$$

$$\sum_{i=1}^n c_i^* = \sum_{i=1}^n c_i + \Phi(D_n) - \Phi(D_0)$$

of flows  $t_i$

$$\Phi(D_i) - \Phi(D_{i-1}) = (b \Phi(D_{i-1}) - t_i + 1) - b \Phi(D_{i-1}) = 1 - t_i$$

$$c_i = c_i + \sum p_i - \sum (D_i) = (t_i + 1) + (1 - t_i) = 2$$

					<u>1</u> <u>merge</u>
	$\sum$	$\sum$	$\sum$	$\sum$	$\sum$
$O(1)$	Amortized	$O(h)$	w.c	$\sum$	$\sqrt{C}$
$O(\log h)$	Amortized	$O(\log h)$	w.c	$\sum$	$\rightarrow$

$\sum \sqrt{h} = \sqrt{N}$

$$O(1) N = O(N) \quad (10)$$

$$O(\log N) N = O(N \log N) \quad (2)$$

				$\sum$
$O(1)$	$\sum$	pop	$(\phi)$	$\sum$
$O(1)$	$\sum$	push	$(\phi)$	$\sum$
$O(\log h)$	$\sum$	pop	$\log()$	$\sum$

Amortized

				$\sum$
	$\sum$	push	<del><math>\sum</math></del>	$\sum$
	$\sum$	pop	$(\phi)$	$\sum$
$O(\log h)$	$\sum$	pop	$\log()$	$\sum$